

# Calcium Leak Induced Sinus Bradycardia

Qingjie Wang<sup>1,2</sup>, Sanjay Kharche<sup>2,3</sup>, Gareth Jones<sup>2</sup>, Cunjin Luo<sup>4,2</sup>, Chengchun Tang<sup>1</sup>,  
Henggui Zhang<sup>2</sup>

<sup>1</sup>Department of Cardiology, Zhongda Hospital of Southeast University, Nanjing, China

<sup>2</sup>School of Physics and Astronomy, University of Manchester, Manchester, M13 9PL, UK

<sup>3</sup>College of Engineering, Mathematics, and Physical Sciences, University of Exeter, EX4 4QF, Exeter, UK

<sup>4</sup>School of Computer Science and Technology, Harbin Institute of Technology, Harbin, China

## Abstract

*Bradycardia is found to be a complication during catecholaminergic polymorphic ventricular tachycardia in which calcium leak plays a pivotal role. In this computational study, we determined the effects of sarcoplasmic reticulum calcium leak on sino-atrial node and ventricular model cells function. A sarcoplasmic reticulum calcium leak current,  $J_{leak}$ , was increased in sino-atrial node and ventricle model cells. The  $J_{leak}$  current is determined by  $v_2$ , the calcium leak rate constant from the net sarcoplasmic reticulum. In the sino-atrial node cell model, the pacing cycle length increased steadily till  $v_2$  values became  $3.1 \times 10^{-5} \text{ ms}^{-1}$ . Further increase of  $v_2$  made pacemaking give rise to long-short, big amplitude-small amplitude oscillations as well as arrest. The amplitude of subspace calcium, calcium diffusion, maximum upstroke velocity of the membrane potential, L-type calcium current and  $\text{Na}^+/\text{Ca}^{2+}$  exchanger current were decreased when  $v_2$  was increased in sino-atrial node cell model. However, the effects of  $J_{leak}$  on ventricular action potential and ionic currents are small. The results show the significance of calcium leak as a major mechanism of sino-atrial node dysfunction.*

## 1. Introduction

Bradycardia is a debilitating cardiac arrhythmia that present in many forms of cardiac disease [1, 2]. Clinical treatment of bradycardia is a significant burden on health care systems [2]. Therefore, it is crucial to understand the mechanisms of this disease to improve clinical therapies.

Ryanodine receptor channels located on the intracellular sarcoplasmic reticulum (SR) regulate intracellular calcium homeostasis [3]. Increased SR calcium ( $\text{Ca}^{2+}$ ) leak increases cytosolic calcium content. The increased  $\text{Ca}^{2+}$  content has apparently paradoxical effects [4]. On

one hand, it is known to lead to sino-atrial node (SAN) bradycardia. On the other hand, it gives rise to ectopic beats and delayed after depolarisations in atrial tissue [5, 6].

However, the mechanisms underlying  $\text{Ca}^{2+}$  leak and arrhythmias are poorly understood. The current study focused on the effects of SR calcium leak by using mouse SAN model [7] and ventricular cell model [8]. The results of simulation showed that increased  $\text{Ca}^{2+}$  leak from SR leading to bradycardia and cardiac arrest in SAN.

## 2. Methods

Detailed mathematical models of mouse sinoatrial node and ventricle electrophysiology were adopted in this study. The SAN cell model published in our laboratory [7] was adopted to reproduce SAN pacemaking. Under control conditions, the SAN model does not encompass a calcium leak from the SR to the cytosol. We therefore modified the model by adding a SR calcium leak current,  $J_{leak}$ , to the calcium dynamics of the model by using the following formulation (Eq.1). The Bondarenko model already has a  $J_{leak}$  component in the calcium dynamics. In the formulation,  $v_2$  is  $\text{Ca}^{2+}$  leak rate constant from the net sarcoplasmic reticulum (NSR),  $\text{Ca}_{up}$  is the  $\text{Ca}^{2+}$  concentration in NSR,  $\text{Ca}_i$  is the  $\text{Ca}^{2+}$  concentration in the cytosol,  $J_{up}$  is  $\text{Ca}^{2+}$  uptake flux from the cytoplasm to the NSR,  $J_{tr}$  is  $\text{Ca}^{2+}$  transfer flux from the NSR to the junctional SR (JSR),  $v_{rel}$  is volume of the JSR,  $v_{up}$  is volume of the NSR,  $v_{sub}$  is volume of the subspace,  $J_{cadif}$  is  $\text{Ca}^{2+}$  diffusion flux from the subspace to the myoplasm,  $v_i$  is the myoplasmic volume available for  $\text{Ca}^{2+}$  diffusion,  $C_m$  is the capacitance,  $J_{trpn}$  is  $\text{Ca}^{2+}$  flux to troponin,  $I_{NaCa}$  is the  $\text{Na}^+/\text{Ca}^{2+}$  exchange current,  $I_{pCa}$  is the  $\text{Ca}^{2+}$  pump current,  $I_{Cab}$  is the background  $\text{Ca}^{2+}$  currents and  $v_{myo}$  is myoplasmic volume.

Eq.1.

Sino-atrial node

$$J_{leak} = v_2(Ca_{up} - Ca_i)$$

$$\frac{d}{dt}Ca_{up} = -J_{leak} + J_{up} - J_{tr}v_{rel}/v_{up}$$

$$\frac{d}{dt}Ca_i = (J_{leak} + J_{Cadif}v_{sub} - J_{up}v_{up})/v_i$$

+ buffering terms.

Ventricle

$$J_{leak} = v_2(Ca_{up} - Ca_i)$$

$$\frac{d}{dt}Ca_{up} = (J_{up} - J_{leak})v_{myo}/v_{up} - J_{tr}v_{rel}/v_{up}$$

$$\frac{d}{dt}Ca_i = bi(J_{leak} + J_{xfer} - J_{up} - J_{trpn} - (I_{Cab} - 2I_{NaCa} + I_{pCa}) \frac{A C_m}{2 v_{myo} F})$$

The model of Bondarenko et al. [8] that simulates ventricle APs was adopted to permit a simulation of mouse ventricle electrophysiology. During pacing of excitable cells by Bondarenko, a stimulus of -80  $\mu A/\mu F$  is applied for a duration of 0.5 ms. The model is paced with a ion charge conservative current stimulus carried by potassium [10]. The SAN and ventricle model were encoded into the Beatbox simulation package as described previously[11].

The model behaviour was studied by increasing the maximum amount of  $J_{leak}$  ( $v_2$ ) in the two models. In a first set of simulations,  $J_{leak}$  was increased from basal values till either SAN pacemaking was affected, or when the excitable cell model demonstrated an increase of action potential duration at 90% of repolarization (APD<sub>90</sub>). The  $J_{leak}$  was then increased and reduced in a large range beyond physiological limits to elicit model behaviour in an extensive range of  $J_{leak}$  conditions. To quantify the effects of  $J_{leak}$ , we observed the characteristics of SR  $Ca^{2+}$ , cytosolic  $Ca^{2+}$ , and AP properties. This included minimum and maximum values during an AP. The AP itself was characterised by minimum diastolic potential, take off potential, peak potential, and APD<sub>90</sub>.

The ordinary differential equations of the two respective models were integrated using a simple forward Euler integration method. The time step for the SAN model was taken to be 0.0025 ms, whereas for the ventricle model was taken to be 0.0001 ms. In both models, measurements were performed on the 100<sup>th</sup> excitation which was assumed to be a steady oscillatory or resting response to the given value of  $J_{leak}$ . The simulations were performed on a standard PC using Ubuntu Linux and GNU C compiler. The figures were prepared using SigmaPlot.

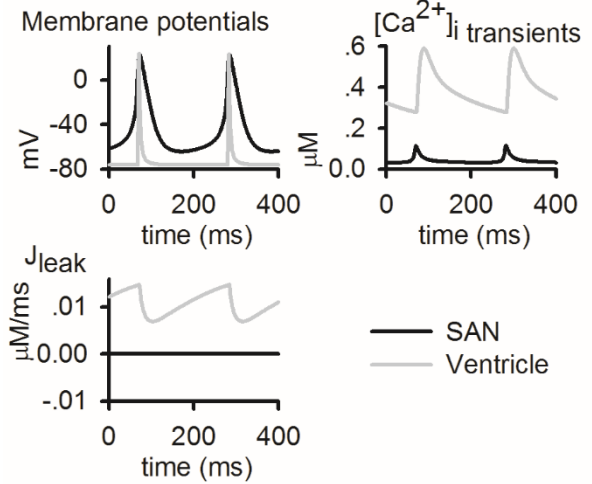


Figure 1. Membrane potential, calcium transient, and SR leak current in the control model. The SAN model has a cycle length of 233.3 ms. The ventricle model has an APD90 of 30 ms. B: The calcium transient in the SAN model is smaller than in the ventricle model. Ventricle has a  $J_{leak}$  at about 0.01  $\mu M/ms$ .

Table 1. Basal cell model properties.

	SAN	Ventricle
CL(SAN)/APD90(Vent), ms	233.3	30
dV/dtmax	8.2 to 32	147
Minimum potential, mV	-60	-75.9
Maximum potential, mV	25	23.7
Take off potential, mV	-48.45	/
Diastolic $Ca_i$ , $\mu M$	0.03	0.25
Systolic $Ca_i$ , $\mu M$	0.11	0.57
Diastolic $Ca_{up}$ , $\mu M$	1734.3	1087.1
Systolic $Ca_{up}$ , $\mu M$	1399.1	1069.0
Peak $I_{CaL}$ , pA/pF	7.2	10.9
Peak $I_{NaCa}$ , pA/pF	2.9	0.11
$J_{leak}$ , $\mu M/ms$	0	0.01

### 3. Results

#### 3.1. Basal model behavior

Control SAN and ventricle membrane potentials are shown in Figure 1. Table 1 shows basal model properties for APs,  $Ca^{2+}$  transients and  $J_{leak}$ . The simulated SAN and ventricle membrane potentials have the same features of isolated mouse SAN and ventricle cells. The SAN and ventricle model produces  $[Ca^{2+}]_i$  oscillations with an amplitude of 0.1  $\mu M$  and 0.6  $\mu M$ , which are close to experimental data [12].

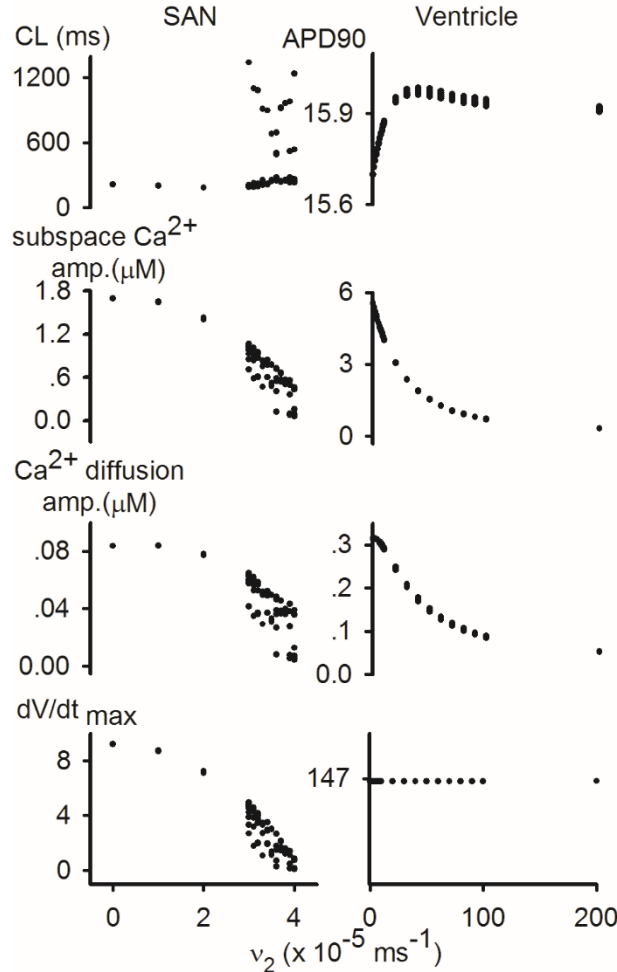


Figure 2. Cycle length (CL), action potential duration 90 (APD90), amplitude of subspace calcium, amplitude of calcium diffusion and  $dV/dt_{max}$  in SAN and/or ventricle model with different  $J_{leak}$ . CL in SAN model increased significantly following increased  $J_{leak}$ , accompanied with decrease of subspace calcium, calcium diffusion and  $dV/dt_{max}$ . In ventricle cell model, subspace calcium and calcium diffusion are also decreased due to increased  $J_{leak}$ . There are no significantly changes of APD90 and  $dV/dt_{max}$  in ventricle by increased  $J_{leak}$ .

### 3.2. AP and $Ca^{2+}$ alterations because of a $J_{leak}$

APs in SAN and ventricle cell model were simulated at various values of  $J_{leak}$ .  $J_{leak}$  is mainly determined by  $Ca^{2+}$  leak rate constant from the NSR ( $v_2$ ) in both SAN and ventricle cell model as shown in Eq.1. As is showed in Figure 2, in the SAN cell, the cycle length (CL) was slightly shortened when  $v_2$  was increased from 0 to  $2 \times 10^{-5} ms^{-1}$ . CL was significantly increased when  $v_2$  is larger than  $3 \times 10^{-5} ms^{-1}$  and AP was arrested when  $v_2$  is larger than  $4 \times 10^{-5} ms^{-1}$ . The amplitude of subspace  $[Ca^{2+}]_i$ ,  $Ca^{2+}$

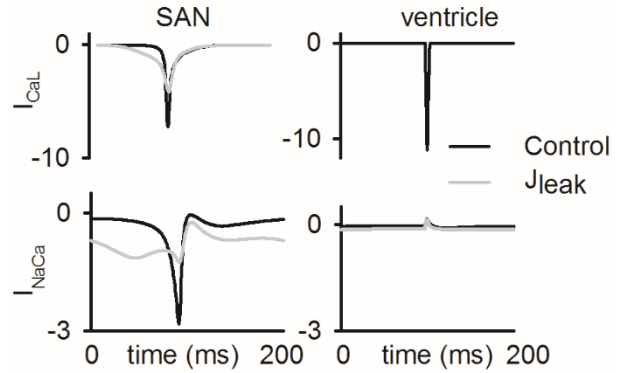


Figure 3. The effects of  $J_{leak}$  on ventricular ionic currents are small. Top panels show change of  $I_{CaL}$  due to increased  $J_{leak}$ . The change in  $I_{NaCa}$  is shown in the bottom panels. The ionic currents during APs are normalized to  $C_m$  (pA/pF).

diffusion and  $dV/dt_{max}$  were decreased when  $v_2$  was increased. However, in ventricle cell model, the APD90 and  $dV/dt_{max}$  were not changed.

In the SAN cell model, the pacing cycle length increased steadily till  $v_2$  values became  $3.1 ms^{-1}$ . Upon further increase of  $v_2$ , the pacemaking became complex and gave rise to long-short as well as big amplitude-small amplitude oscillations. This is reflected in our observation of several apparently random CLs in the SAN oscillations for  $v_2 > 3.1 \times 10^{-5} ms^{-1}$ . In contrast, in the ventricle cell, as  $v_2$  was increased, the APD90 did not change significantly. It reduced from the basal 15.9 ms to 15.8 ms. However, as  $v_2$  was reduced, the APD90 reduced by 2%. As  $J_{leak}$  was increased, the SR  $Ca^{2+}$  content reduced in both cell types. It reached 0 at  $v_2 = 4 \times 10^{-5} ms^{-1}$  in the SAN, and at  $v_2 = 1 \times 10^{-3} ms^{-1}$  in the ventricle cell model. The  $Ca^{2+}$  amplitude followed a similar pattern to the SR  $Ca^{2+}$  behavior. An important observation that we saw was that the SAN upstroke velocity was very sensitive to the  $J_{leak}$  parameter, whereas in case of the ventricle model it was the contrary.

Figure 3 shows the effects of  $J_{leak}$  on L-type  $Ca^{2+}$  current ( $I_{CaL}$ ) and  $Na^+/Ca^{2+}$  exchanger current ( $I_{NaCa}$ ). Under basal conditions, the  $I_{CaL}$  has a peak of -10 pA/pF in both cell types. The  $I_{NaCa}$  is large in the SAN model (peak of -3 pA/pF), whereas it is small in the ventricle model. These are the two major membrane currents that are affected by cytosolic  $Ca^{2+}$ . In SAN model, both  $I_{CaL}$  and  $I_{NaCa}$  were decreased due to increased  $J_{leak}$  ( $v_2 = 2 \times 10^{-5} ms^{-1}$ ). However, in ventricle cell model,  $I_{CaL}$  and  $I_{NaCa}$  were not affected by increased  $J_{leak}$  ( $v_2 = 2 \times 10^{-3} ms^{-1}$ ).

## 4. Conclusions and discussion

This simulation study shows that SR  $Ca^{2+}$  leak affects several electrophysiological components in the cell

models. Overall, increase of  $\text{Ca}^{2+}$  leak was seen to cause arrhythmic alterations in the cytosolic  $\text{Ca}^{2+}$  concentrations which led to drastic alterations in the electrophysiological behavior. In contrast, an increase of  $\text{Ca}^{2+}$  leak in the ventricle cell affected the intracellular content while the cell membrane electrophysiology remained unaltered. In the SAN cell, the cytosolic  $\text{Ca}^{2+}$  is strongly coupled to the cell membrane electrophysiology. This is due to the strong dependence of  $I_{\text{CaL}}$  inactivation, as well as  $I_{\text{NaCa}}$  function on  $[\text{Ca}^{2+}]_i$ . As these currents are major contributors to SAN cell upstroke ( $I_{\text{CaL}}$ ) and to the slow depolarization phase ( $I_{\text{NaCa}}$ ), In contrast, the  $[\text{Ca}^{2+}]_i$  in the ventricle cell increases due to the an increasing leak. However, the coupling of the cytosolic calcium in this model is significantly smaller than in the SAN cell. Therefore, the membrane electrophysiology remains largely unaltered as seen in Figure 2. The results is useful to illustrate the mechanism of bradycardia during CPVT.

Previous studies have reported that patients with CPVT have SAN dysfunction [4]. SAN automaticity is regulated by the voltage clocks and  $\text{Ca}^{2+}$  clock [13]. The simulation results showed that SR  $\text{Ca}^{2+}$  leak causes decreased subspace  $\text{Ca}^{2+}$  concentration, reduces the state of  $\text{Ca}^{2+}$  overload, thus decreases the automaticity of SAN. Moreover, the downregulation of  $I_{\text{CaL}}$  caused by increased  $J_{\text{leak}}$  could reduce the slope of phase 0 and reduce the heart rate.

## Acknowledgements

QW and CL were supported by China Scholarship Council. SK was supported by an EPSRC (BeatBox grant) and British Heart Foundation Grant. CT was supported by National Natural Science Foundation of China (No.81170105, No. 81370225).

## References

- [1] Lewalter, T., Luderitz, B. Atrial fibrillation: mortality, morbidity, and money; is that all? Importance and variability of burden measurement. *European heart journal* 26, 110-111 (2005)
- [2] Arribas, F., Auricchio, A., Boriani, G., Brugada, J., Deharo, J.C., Hindriks, G., Kuck, K.H., Merino, J.L., Vardas, P., Wolpert, C., Zeppenfeld, K. Statistics on the use of cardiac electronic devices and electrophysiological procedures in 55 ESC countries: 2013 report from the European Heart Rhythm Association (EHRA). *Europace : European pacing, arrhythmias, and cardiac electrophysiology : journal of the working groups on cardiac pacing, arrhythmias, and cardiac cellular electrophysiology of the European Society of Cardiology* 16 Suppl 1, i1-78 (2014)
- [3] Berridge, M.J., Bootman, M.D., Roderick, H.L. Calcium signalling: dynamics, homeostasis and remodelling. *Nature reviews. Molecular cell biology* 4, 517-529 (2003)
- [4] Neco, P., Torrente, A.G., Mesirca, P., Zorio, E., Liu, N., Priori, S.G., Napolitano, C., Richard, S., Benitah, J.P., Mangoni, M.E., Gomez, A.M. Paradoxical effect of increased diastolic  $\text{Ca}^{2+}$  release and decreased sinoatrial node activity in a mouse model of catecholaminergic polymorphic ventricular tachycardia. *Circulation* 126, 392-401 (2012)
- [5] Priori, S.G., Chen, S.R. Inherited dysfunction of sarcoplasmic reticulum  $\text{Ca}^{2+}$  handling and arrhythmogenesis. *Circulation research* 108, 871-883 (2011)
- [6] Lakatta, E.G., DiFrancesco, D. What keeps us ticking: a funny current, a calcium clock, or both? *Journal of molecular and cellular cardiology* 47, 157-170 (2009)
- [7] Kharche, S., Yu, J., Lei, M., Zhang, H. A mathematical model of action potentials of mouse sinoatrial node cells with molecular bases. *American journal of physiology. Heart and circulatory physiology* 301, H945-963 (2011)
- [8] Bondarenko, V.E., Szegedi, G.P., Bett, G.C., Kim, S.J., Rasmusson, R.L. Computer model of action potential of mouse ventricular myocytes. *American journal of physiology. Heart and circulatory physiology* 287, H1378-1403 (2004)
- [9] Bondarenko, V.E. A compartmentalized mathematical model of the beta1-adrenergic signaling system in mouse ventricular myocytes. *PloS one* 9, e89113 (2014)
- [10] Hund, T.J., Kucera, J.P., Otani, N.F., Rudy, Y. Ionic charge conservation and long-term steady state in the Luo-Rudy dynamic cell model. *Biophys J* 81, 3324-3331 (2001)
- [11] Kharche, S., Beling, J., Biktasheva, I.V., Zhang, H., Biktashev, V.N. Simulating cell apoptosis induced sinus node dysfunction. *Conference proceedings : ... Annual International Conference of the IEEE Engineering in Medicine and Biology Society. IEEE Engineering in Medicine and Biology Society. Annual Conference* 2013, 6842-6845 (2013)
- [12] Kurata, Y., Hisatome, I., Imanishi, S., Shibamoto, T. Dynamical description of sinoatrial node pacemaking: improved mathematical model for primary pacemaker cell. *American journal of physiology. Heart and circulatory physiology* 283, H2074-2101 (2002)
- [13] Joung, B., Chen, P.S., Lin, S.F. The role of the calcium and the voltage clocks in sinoatrial node dysfunction. *Yonsei medical journal* 52, 211-219 (2011)

Addresses for correspondence.

Prof. Henggui Zhang.  
University of Manchester, M13 9PL, UK.  
henggui.zhang@manchester.ac.uk