

# Effects of Acute Ischemia and Its Components on the Safety Factor of Conduction: A Simulation Study

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## Abstract

*In this work, we have studied the changes that acute myocardial ischaemia exerts in our formulation of the safety factor of conduction ( $SF_m$ ) which consists on a modification of the SF proposed by Shaw and Rudy. Specifically, the effect of each component of ischemia (hyperkalemia, hypoxia and acidosis) was studied separately, and also the evolution of the  $SF_m$  after the onset of ischemia was obtained.*

*The results show that a) the three components of ischemia tend to reduce  $SF_m$  (except mild hyperkalemia), with strong hyperkalemia being the most important one and with hypoxia playing a mayor role only at high extracellular K concentration ( $[K^+]_o$ ), and b) the  $SF_m$  decreases continuously as ischemia progresses.*

## 1. Introduction

As many potentially mortal cardiac arrhythmias, such as ventricular tachycardia (VT) and ventricular fibrillation (VF), are normally caused by a failure in the cardiac impulse [1], much attention has been paid to the evaluation of safeness of the propagation of the electrical impulse [2]. Recently, a quantitative parameter, called safety factor (SF), has been used for this purpose [2].

It is well known that acute myocardial ischemia facilitates the appearance of VT and VF [1]. Indeed, the electrophysiological changes that occur during acute ischemia profoundly affect the action potential (AP) conduction characteristics. Among these changes, it is worthy to mention the reduction of the membrane excitability [3], and decrease of the depolarization velocity [4] and the prolongation of the refractory period.

As VT and VF normally take place in acute ischemia, we have simulated the three main components of ischemia separately to analyse the changes that each of them provokes on our formulation of the SF ( $SF_m$ ), and we have also reproduced the situation at 0, 5 and 10 minutes after the onset of ischemia to study the evolution of this parameter.

## 2. Methods

The electrical activity of an homogeneous 160-cell strand has been simulated using a modified version of the 2000 Luo-Rudy action potential model [5].

Acute ischaemia has been mimicked by means of its three components, hyperkalemia, hypoxia and acidosis. The simulations were defined in a way that tries to reproduce the evolution of ischemia. The parameters affected by the components of ischemia were assigned the values registered experimentally (Table 1). Firstly, hypoxia was taken into account by partially activating the ATP-sensitive  $K^+$  current ( $I_{K(ATP)}$ ), which was formulated as Ferrero Jr. et al. [4] and intracellular values of ATP and ADP ( $[ATP]_i$  and  $[ADP]_i$ ) were comprised in the range 6.8-4.6 mmol/L and 15-199  $\mu$ mol/L respectively [6,7]. Secondly, hyperkalemia was considered by elevating extracellular  $K^+$  concentration ( $[K^+]_o$ ), specifically,  $[K^+]_o$  was set to a value in the range 5.4-12.5 mmol/L [7,8]. Finally, acidosis was accounted by means of a multiplicative factor ( $f_{pH}$ ) that reduces up to a 25 % the fast inward  $Na^+$  current ( $I_{Na}$ ) and the  $Ca^{2+}$  current through the L-type channels ( $I_{Ca(L)}$ ) [9,10].

	Normoxia	5 min	10 min
	Onset of	after the onset	after the onset
	ischemia	of ischemia	of ischemia
$[K^+]_o$	4.5 mM	12 mM	12 mM
pH	7.4	6.9	6.4
$f_{ATP}$	0 %	0.25 %	0.25 %

Table 1. Significant parameters affected by acute ischemia and its corresponding values for the selected instants after the occlusion of the coronary artery.

Different tissue conditions were simulated: one subgroup of simulations considered each component of ischaemia separately, while other subgroup mimicked conditions after 0, 5, and 10 minutes of myocardial

ischemia.

The fiber was stimulated by a train of 10 driven rectangular pulses of a basic cycle length of 500 ms, 2 ms in duration and twice diastolic threshold current in amplitude. This current was applied in one edge of the fiber and the  $SF_m$  was calculated for the last AP.

### 3. Results

The influence in the  $SF_m$  of each component of ischemia separately is shown in Figure 1. Firstly, the results show that hyperkalemia produces a biphasic behaviour in the  $SF_m$  (Figure 1.A). Small increments in  $[K^+]_o$  slightly augment the normal  $SF_m$  value (1.606), reaching a maximum of 1.666 at 7.5 mM, but below that  $[K^+]_o$   $SF_m$  begins to decrease, reaching a value of 1.122 at 14.6 mM. This biphasic behaviour is in accordance with other experimental [11] and theoretical [12] studies. Secondly, as depicted in Figure 1.B, acidosis tends to decrease the  $SF_m$ , as the more reduced the membrane excitability, the fewer the value of registered  $SF_m$ . Indeed, 1.276 is the value of  $SF_m$  when  $I_{Na}$  and  $I_{Ca(L)}$  are reduced by 20% ( $f_{pH} = 20\%$ ). The reduction of the  $SF_m$  with increasing inexcitability is foreseeable, as propagation of the impulse becomes more difficult as inexcitability of a tissue augments. Thirdly, as reflected in Figure 1.3, it seems clear that hypoxia by itself produces a very slight decrement on the  $SF_m$  so it can be considered that hypoxia has a negligible influence on the  $SF_m$ . So, we conclude that the three components of ischemia by themselves decrement the  $SF_m$ , except mild hyperkalemia.

The appearance of failure in the electrical conduction when combining the components of ischemia has also been analysed. On one hand, we have combined a realistic level of acidosis during ischemia ( $I_{Na}$  and  $I_{Ca(L)}$  reduced to 75%) with hyperkalemia, and we have found that propagation failure ( $SF_m < 1$ ) occurs at  $[K^+]_o = 13.55$  mM. On the other hand, when moderate hypoxia ( $f_{ATP} = 0.5\%$ ) was also added to acidosis (75%  $I_{Na}$  and  $I_{Ca(L)}$  reduction)  $SF_m$  drops below unity at  $[K^+]_o = 12$  mM. Therefore, hypoxia plays a major role at high  $[K^+]_o$ , despite having a negligible effect for moderated  $[K^+]_o$ .

All in all, it seems clear that the three components of ischemia tend to reduce  $SF_m$  (except mild hyperkalemia), with strong hyperkalemia being the most important one and with hypoxia playing a mayor role only at high  $[K^+]_o$ .

Finally, regarding the evolution of  $SF_m$  during ischemic episodes, this parameter reaches a value of 1.393 five minutes after the onset of ischemia, becoming 1.263 after 10 minutes. So the  $SF_m$  decreases continuously as ischemia progresses.

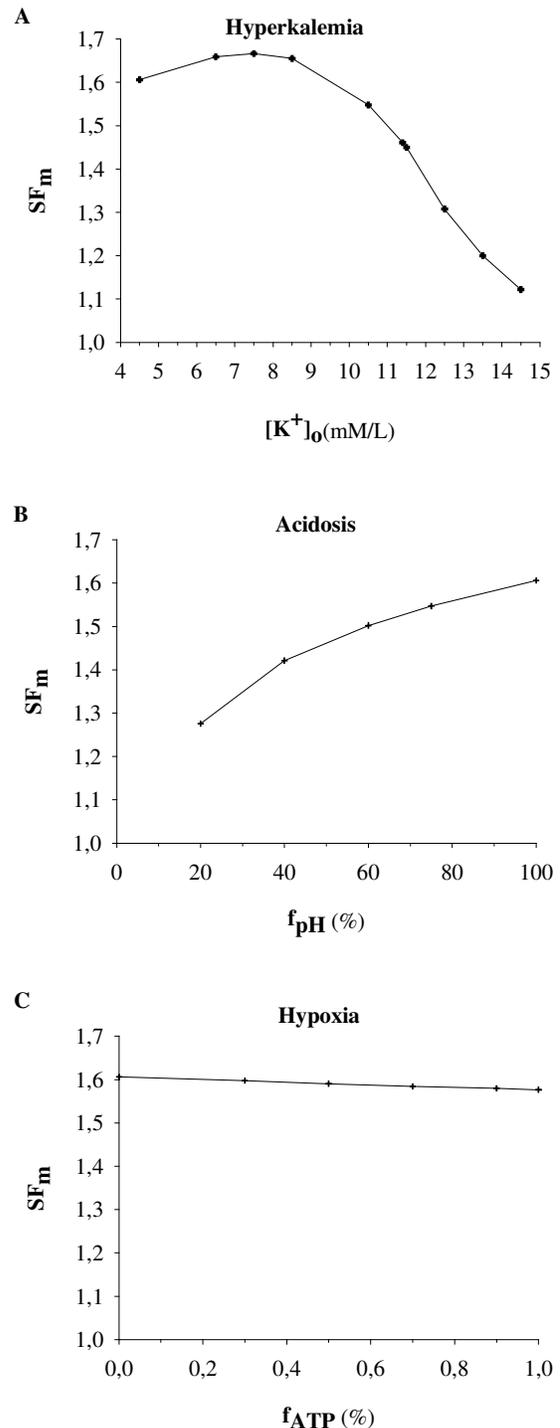


Figure 1. Effect of each component of ischemia on the  $SF_m$  separately. A) Hyperkalemia, B) Acidosis ( $f_{pH}$  is the factor that reduces  $I_{Na}$  and  $I_{Ca(L)}$  and it depends on the pH) and C) Hypoxia ( $f_{ATP}$  is the fraction of activated K(ATP) channels, this parameter is determined by  $[ATP]_i$  and  $[ADP]_i$ .)

## 4. Conclusions

Some papers have considered the study of the SF under different conditions, but the interest of this work lies on the fact that the effect of the main components of acute ischemia on the SF<sub>m</sub> has been considered.

This study tries to throw a light on the effects of acute ischemia on the SF<sub>m</sub> by analysing not only the contribution of each component of ischemia to both SF<sub>m</sub> and appearance of the conduction failure, but also the evolution of this indicator after the onset of ischemia.

Our results show that a) the three components of ischemia tend to reduce SF<sub>m</sub> (except mild hyperkalemia), with strong hyperkalemia being the most important one and with hypoxia playing a mayor role only at high [K<sup>+</sup>]<sub>o</sub>, and b) the SF<sub>m</sub> decreases continuously as ischemia progresses.

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