

# Heart Attack Outcome Predictions Using FMM Models

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## Abstract

*As part of the PhysioNet Challenge 2023, our team FM-MGroup\_UVa presents an original approach for the prediction of the outcome of coma patients after a heart attack. Our methodology involves the integration of two types of EEG features extracted from 10-second epoch data, analyzed at various time intervals with patient clinical data. The first type is the FMM features created from the parameters of an FMM (Frequency Modulated Möbius) model fitted to the epoch data. The other type is indices taken from the literature that include spectral, entropy, and background measures. The mean feature values for patients are combined with clinical variables into classification models to obtain an outcome score in a given time block. Our best performance in the official challenge phase achieved a score of 0.45 at 72 hours on the test dataset. Additionally, we introduce an alternative proposal in this paper, displaying promising results in our laboratory. Unfortunately, this proposal was not ranked due to difficulties in submitting it on time without errors.*

## 1. Introduction

The FMM approach is among the more interesting recent advancements in mathematical modeling techniques for the analysis of single-channel and multi-channel bioelectric signals. It has been successfully used to analyze electrocardiograms, neuronal spikes, or electroretinograms, among other biological signals [1,2]. FMM models for single channels are formulated as a sum of components defined in terms of four parameters. When multi-channel data is analyzed the individual components are connected, in such a way that there exists a set of parameters that are common to all channels, as well as other parameters that are channel-specific. As a result, the calculation of indices measuring channel-specific features and connectivity measures across channels is easily addressed. Moreover, the model parameters capture the morphology of the fundamental waves present in the signals and thus are easily interpretable and have great potential in tasks such as classification or prediction [2].

In addition, the FMM approach can effectively analyze signals regardless of the preprocessing steps applied, the

type of recording device used, or the number of channels involved. These issues make the FMM approach versatile and adaptable to various data acquisition set-ups and conditions.

In this paper, we propose to derive helpful FMM features in the prediction outcomes of coma patients who suffered a heart attack [3–5]. This is the first time the FMM approach is used for EEG data analysis. For the aim of this paper, we propose extracting 10 components from each 10-second epoch. The rationale behind this strategy is rooted in the representation of slow waves, a well-documented phenomenon in the scientific literature. Slow waves, often referred to as delta waves, manifest as low-frequency, high-amplitude oscillations in the EEG. These distinctive electrical patterns are frequently associated with various sleep stages and periods of reduced neural activity. They reflect the synchronization of neural activity in large populations of neurons. Importantly, alterations in slow-wave activity can serve as indicators of brain injury or neurological disorders, as previously noted [6, 7]. Furthermore, 10-second epochs are commonly used as a standard unit of analysis in most studies. Moderately pronounced spiked components, indicative of slow waves, will be more prevalent in patients with favorable prognoses.

We create features using statistics from the FMM parameters that capture EEG core aspects for the prognosis, such as amplitude, complexity, connectivity, regularity, or spike counting. On the other hand, we also consider spectral, entropy, and background features [8–11]. Table 1 summarizes the features.

The patient average values for such features are combined with clinical variables included in classification models to obtain an outcome score in a given time block.

## 2. Methods

We assume that a raw digital EEG signal (time (seconds), voltage (microvolts)) is available for 18 bipolar channels. Occasionally, the voltage values are not the original ones but they have been scaled in some form. The challenge provided data over a 72-hour period. Our proposal can be described in three steps: the epoch selection, the creation of epoch-level features, and the development of patient classification models. Figure 1 illustrates the

Level	Type	Name	Statistics/Description	$N^o$
Epoch	FMM	$\alpha$	Circular $SD_i(\alpha_i)$ Watson test $\#\{\omega_l < 0.01\}$	2
		$\omega$	$SD_l(\omega_l)$ $CV_l(\omega_l)$	3
		$A$	$ME_c(ME_l(A_{lc}))$ $CV_c(ME_l(A_{lc}))$	2
		$R^2$	$ME_c(ME_l(R_{lc}^2))$	1
		Binary rule	Features outside the percentile healthy range	1
Epoch	Entropy	Shannon	Individual values, Mean, SD	20
		Fractal dimension [11, 12]	Individual values, Mean, SD	20
	Spectral	$\delta, \theta, \alpha, \beta$ Frequency bands[8]	Individual values, Powers, Ratios.	126
		Background	BCI[9], BSAR[9]	Mean, SD
Patient	Clinical	Age, ROSC, Shockable rhythm	Individual values	3

Table 1: List of features by level and type.  $ME$ : median;  $SD$ : standard deviation and  $CV$ : variant coefficient.  $N^o$ : feature counts.

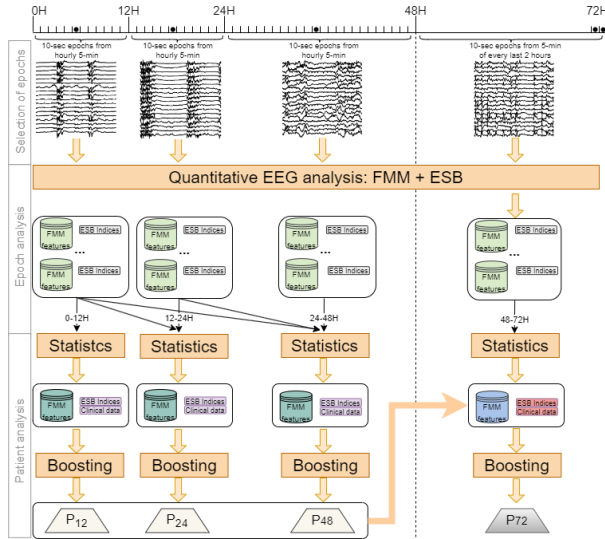


Figure 1: FMMGroup\_UVa flowchart.

steps. Different strategies are designed within this general scheme. The fundamental keys of each step and the strategies considered are commented on below.

### 2.1. Selection of epochs

One pressing issue we have encountered is that the process of generating features is notably time-intensive. Furthermore, it is advisable to not select epochs of exceptionally low quality. Consequently, to remain competitive in the challenge, we found it necessary to fine-tune our algorithm to fit within the allotted computing time. A pivotal aspect of this adaptation involves the selection of epochs,

which distinguishes our different solutions. One straightforward approach involved choosing a 5-minute window from the central portion of the last hour for each patient, and this yielded promising results over the course of 72 hours. Alternatively, we considered utilizing 5-minute segments from each hour for each patient. A solution combining both strategies produced the most favorable outcomes in our laboratory experiments. Moreover, distorted epochs can be identified and eliminated using a simplified version of the EEG quality measure software borrowed from the Challenge. The reason for using a simplified version is again to reduce the computational time.

### 2.2. FMM: model and features

The FMM model considered assumes that the voltage in a time point  $t$  for a given channel ( $c$ ) is a combination of 10 parametrized components or waves ( $l$ ), as follows:

$$\sum_{l=1}^{10} A_{lc} \cos \left( \beta_{lc} + 2 \arctan \left( \omega_l \tan \left( \frac{t - \alpha_l}{2} \right) \right) \right).$$

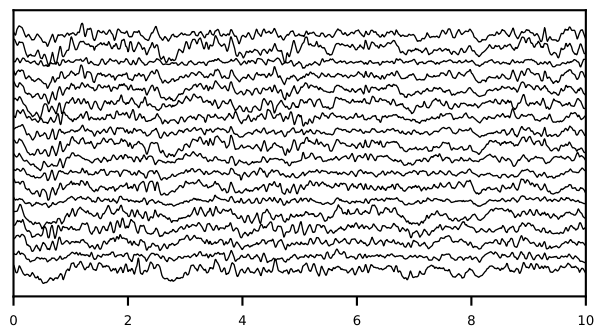
Where,  $A_{lc} \in \mathbb{R}^+$  is an amplitude parameter that measures the height of the waveform  $l$  in channel  $c$ , a proxy for the voltage or signal intensity.  $\alpha_l \in [0, 2\pi)$  is a location parameter that identifies the time in  $[0, 10]$  where the waveform  $l$  spikes.  $\beta_{lc} \in [0, 2\pi)$  and  $\omega_l \in [0, 1]$  describe the waveform shape. Specifically,  $\omega_l$  is related to the width of the waveform  $l$  and to the frequency band. A spiked waveform is described with  $\omega$  values close to 0, while  $\omega$  close to 1 represents a wave lasting exactly 10 seconds.

The role of FMM parameters characterizing epochs is exemplified through the data presented in Figures 2 and 3. In particular, there are differences in the amplitude ( $A$ ), width ( $\omega$ ), and wave locations (Watson statistic test), being these values higher for the case of less favorable prognosis (Figure 3).

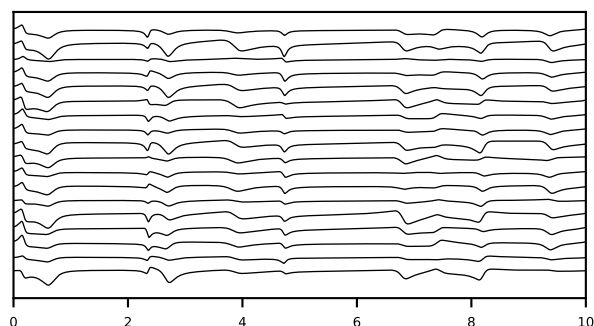
The observed voltages are used to estimate the model parameters for each epoch. We have adopted an approximation estimation algorithm different from that in the mentioned papers to reduce the computing time. In addition to the FMM parameters, we also consider the percentage of variance explained by the model,  $R_{lc}^2$ , for component  $l$  and channel  $c$ . The reader interested can see the papers on the topic [1, 2].

### 2.3. Patient classification models

A large collection of statistics from the estimates of parameters  $A, \alpha$ , and  $\omega$  have been calculated from values across channels and components for each epoch to create features. These include medians, percentiles, variability measures, and others. The FMM features that have proved to be of relevance in classification models are listed in Table 1. Furthermore, we have also considered ESB (Entropy, Spectral, and Background) indices, see Table 1. For



(a) EEG data



(b) FMM prediction

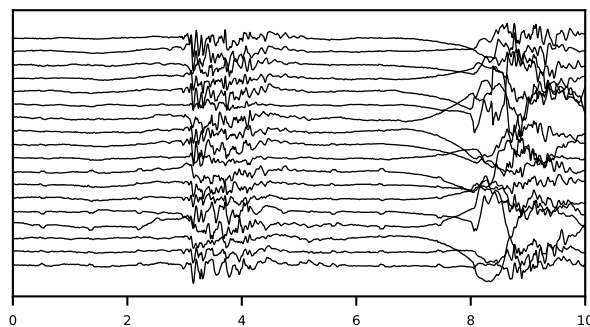
Figure 2: Typical 10-second epoch 18 channels of a patient with favorable prognosis.

a given patient and time block, mean and standard deviation values, across epochs, of selected features have been calculated and have been included in classification models. We have considered logistic regression, gradient boosting, or random forest as classification models.

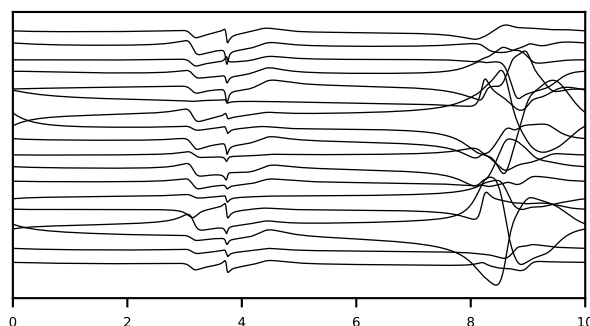
## 2.4. Strategies

Based on this scheme, we have explored various strategies that differ in terms of epoch selection, feature sets, and classification models. In this paper, we present two of them labeled as Strategy A and B.

Strategy A involves selecting all epochs from the central 5 minutes of the last hour of each patient. Feature selection comprises a preliminary binary epoch classifier using a set of FMM features, spectral features, as well as clinical variables. We constructed a random forest model using these selected features. On the other hand, in Strategy B (the recommended approach), the predictions obtained at 12, 24, and 48 hours are derived using the information of FMM and ESB indices of epochs available until that moment. We computed patient scores using boosting classification models that integrate FMM features and a selection of ESB indices, both detailed in Table 1. Additionally, pre-



(a) EEG data



(b) FMM prediction

Figure 3: Typical 10-second epoch 18 channels of a patient with non-favorable prognosis.

dictions at 72 hours are derived by combining FMM features with a second set of selected ESB indices from the last two hours epochs within the 48-72 hour period. Boosting classification model incorporates these features in conjunction with clinical variables and predictions made at 12 hours, 24 hours, and 48 hours.

## 2.5. Results

We have conducted in our laboratory a comparative analysis of the two strategies which includes information from 603 patients following the Challenge rules. We have executed five experiments, each employing a 10-fold cross-validation approach.

The results for Strategy A have been computed for training, validation, and test dataset (see Table 2) along with our validation experiments (see Table 3). The true positive rate (TPR) for predicting a poor outcome given a false positive rate (FPR) of less than or equal to 0.05 at 72 hours after return of spontaneous circulation were 0.642 and 0.450 in the validation and test datasets, respectively. Regrettably, we did not arrive on time to achieve official Challenge scores for Strategy B. Nevertheless, we succeed in comparing both strategies in our laboratory experiments.

The scores obtained for Strategy B significantly outperform those for Strategy A. Crucially, the laboratory scores match with the official score for the test for Strategy A, which enhances the credibility of the laboratory experiment for validation. Furthermore, this alignment allows us to compare the scores of Strategy B with those of other teams, highlighting that Strategy B’s scores at 12 hours surpass all other proposals.

Table 2: TPR and ranking at 72 hours for Strategy A on the training, validation, and test.

	Training	Validation	Test
TPR	0.877	0.642	0.450
Rank	16	7	22

Table 3: TPR mean (SD) laboratory validation scores.

Strategy	Time block			
	12	24	48	72
A	0.236 (0.031)	0.226 (0.021)	0.324 (0.035)	0.442 (0.033)
B	0.441 (0.032)	0.448 (0.041)	0.566 (0.021)	0.611 (0.015)

### 3. Conclusions

Strategy A achieved scores of 0.642 and 0.450 on the validation and test datasets, respectively. While we do not have the score for Strategy B. In our laboratory experiments, Strategy B outperforms Strategy A with scores of 0.442 and 0.611, respectively. Specifically, the scores for Strategy B at 12 hours are notably impressive. This makes it a particularly promising choice, particularly during the initial hours. Furthermore, this paper highlights the utility of the FMM approach in EEG data analysis, with a specific emphasis on demonstrating the predictive potential of these FMM features. Moreover, our proposal is original, marking the inaugural utilization of the FMM approach in EEG analysis. Once we have all the available data, a full comprehensive analysis will be conducted. This analysis will encompass the identification of anomalous epochs and the FMM analysis of all epochs with sufficient quality. With all this documentation in hand, we will once again compare the various proposals presented in this paper through validation experiments employing 10-fold cross-validation.

Furthermore, we will conduct a specific analysis of binary epoch classifiers based on FMM features and assess the predictive capability of other promising features, including those generated from  $\beta$  parameters, among others.

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